

Small-Angle X-ray Scattering – a (mainly) practical introduction: “Where and how to measure SAXS?”

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Outline

Recapitulation

Common SAS camera types

- Characteristic parameters

- Line-focus Kratky camera

- Point focus (pinhole) camera

Main components

- Radiation source

 - X-ray tube

 - Synchrotron

- Collimation

- Sample environment

- Beam stop

- Detector

Two example instruments

- Laboratory SAXS – CREDO

- Synchrotron SAXS – B1 („JUSIFA”)

Scheme of an experiment

- Data acquisition

- Corrections and calibrations

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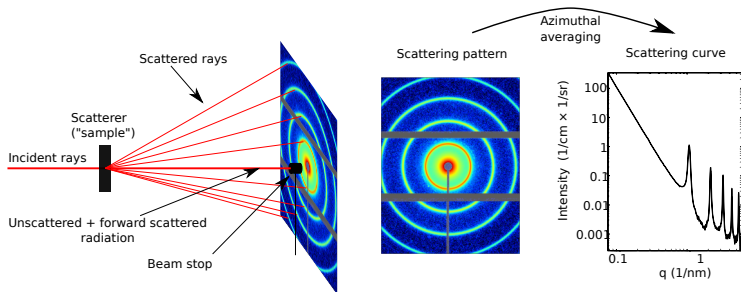
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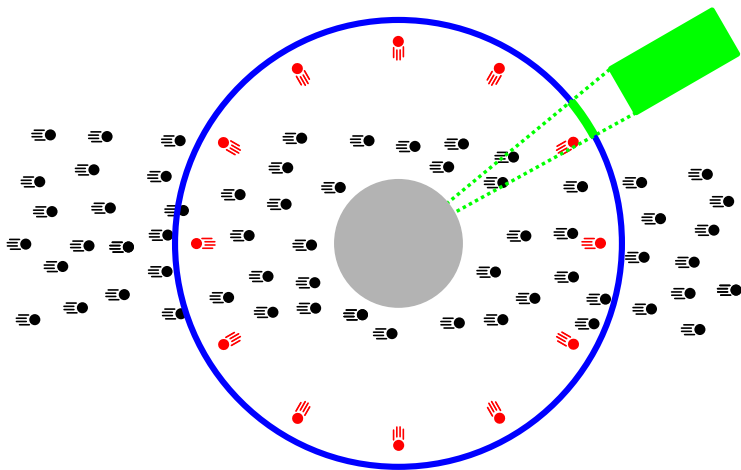
Summary

Scattering experiments



- ▶ Scattering of X-rays on the matter
- ▶ Scattering pattern \rightarrow scattering curve

Intensity

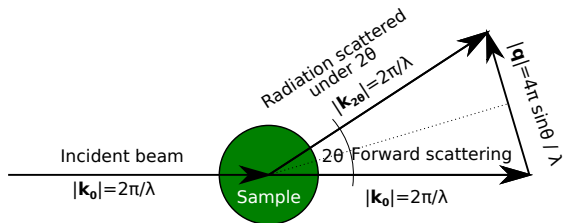


Relative intensity: the number of “event” detected during the measurement

Absolute intensity: differential scattering cross-section:

$$d\sigma/d\Omega = I_{\text{in}}/|J_{\text{out}}|$$

Angle-dependence

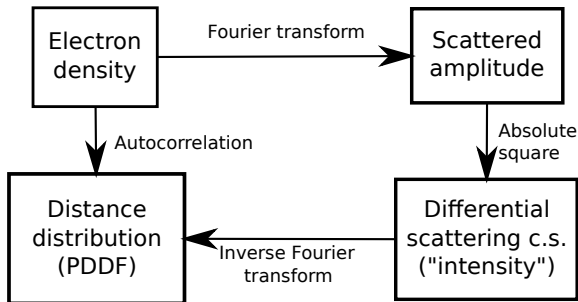


Scattering vector: $\vec{q} = \vec{k}_{2\theta} - \vec{k}_0$, $q = 4\pi \sin \theta / \lambda$

Physical meaning: The momentum acquired by the photon in the process
($h\lambda = p$)

Real-space equivalent: Periodic repeat distance via Bragg's equation:
 $q = 2\pi n/d$, $n \in \mathbb{N}$

Connection between structure and scattering



- ▶ Electron density function ($\rho(\vec{r})$)
- ▶ Fourier transform
- ▶ Absolute square \rightarrow phase problem
- ▶ Back to the real space: PDDF

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Final goal: measure weakly scattering samples in short times

X-ray beam

- ▶ High flux
- ▶ Highly parallel (divergence $\ll 1$ mrad)
- ▶ Monochromatic ($\Delta\lambda/\lambda$)

Angular resolution

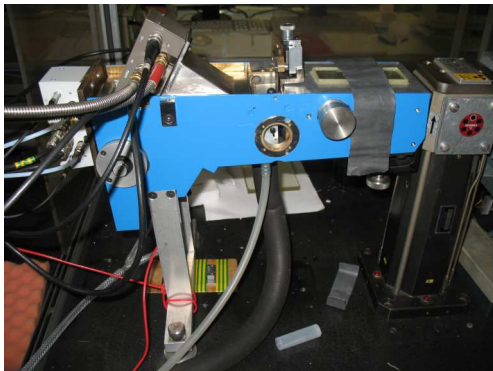
- ▶ Sample-to-detector distance
- ▶ Shape and size of the detector area
- ▶ Pixel size

Noise

- ▶ Electronic noise from the detector
- ▶ Parasitic scattering (comes from the X-ray source, scattered, but not by the sample)
- ▶ External radiation

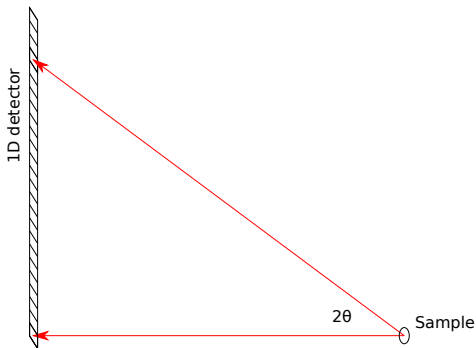
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- ▶ Compact, small footprint
- ▶ 1D position sensitive detector
- ▶ Fixed sample-to-detector distance
- ▶ No moving parts



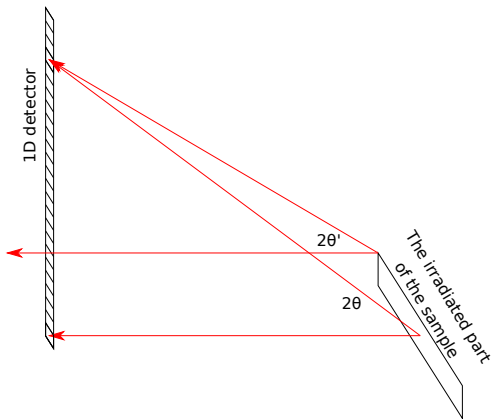
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- ▶ Typical beam size: $2\text{-}3\text{ cm} \times <1\text{ mm}$
- ▶ High intensity on the sample but smearing on the scattering curve



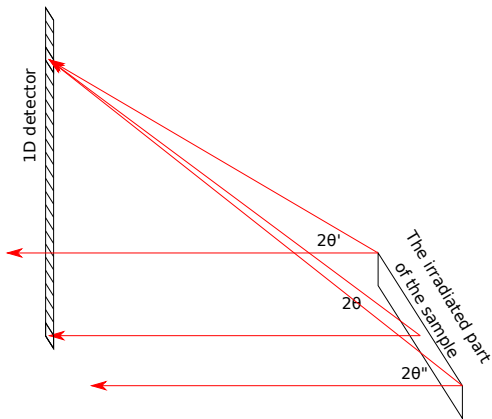
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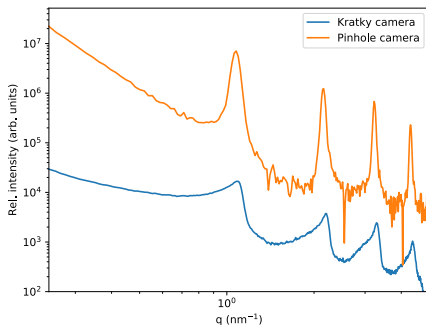
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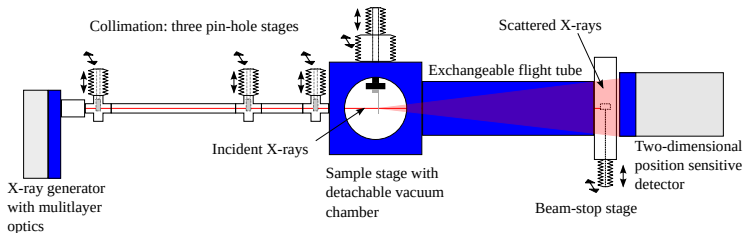


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Point focus (pinhole) camera



- ▶ Small beam size (<1 mm), low divergence
- ▶ Exchangeable sample-to-detector distance: tuning of the angular range
- ▶ Negligible smearing, typically no correction needed
- ▶ Easy to set up and align (compared to the Kratky block)
- ▶ Larger footprint but more possibilities
- ▶ Not (just) a “routine” instrument

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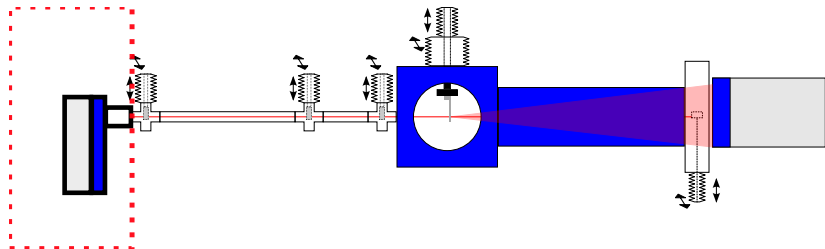
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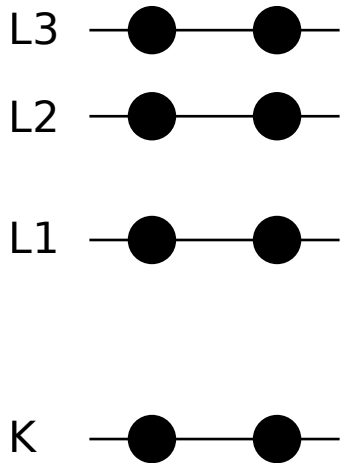
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Radiation source

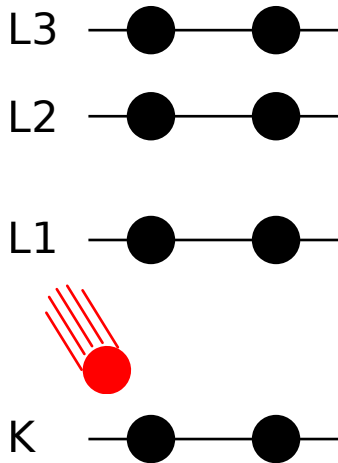


Characteristic X-radiation



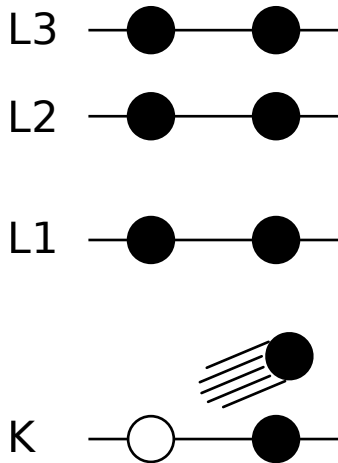
Characteristic X-radiation

- ▶ Excitation of the electronic shell with high-energy particles



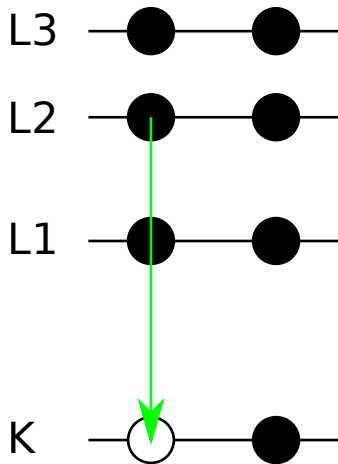
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- ▶ Excitation of the electronic shell with high-energy particles
- ▶ An electron is freed and exits



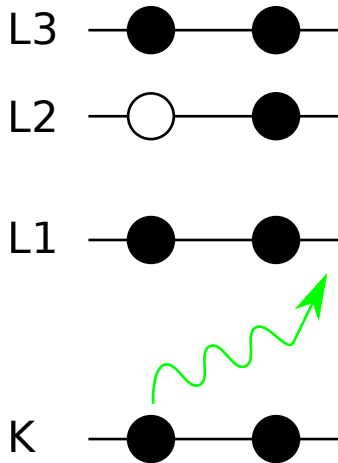
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- ▶ Excitation of the electronic shell with high-energy particles
- ▶ An electron is freed and exits
- ▶ The remaining hole is filled by an electron from an outer shell



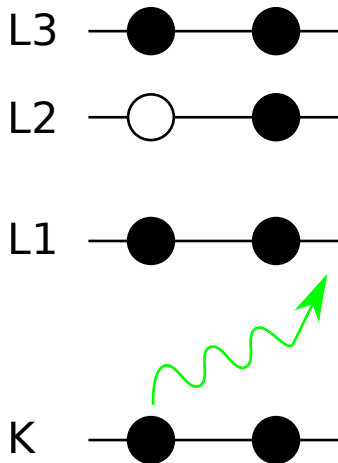
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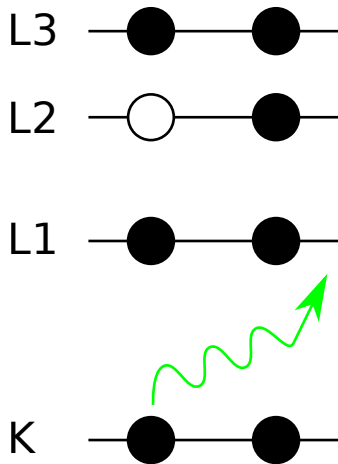
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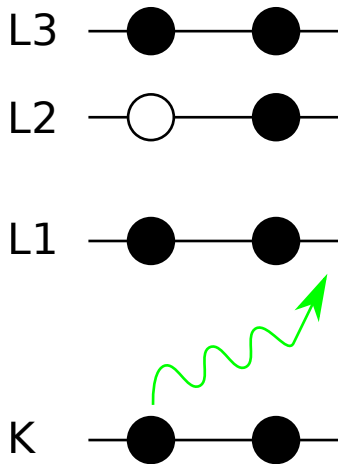
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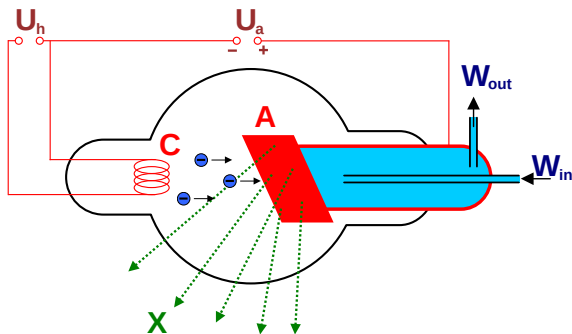


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- ▶ $\Rightarrow h\nu < E_{in}$



How an X-ray tube works?



- ▶ Cathode (C): heated filament, electrons exit due to the thermionic effect
- ▶ U_a : accelerating voltage (40-100 kV): electrons accelerate towards the anode
- ▶ Anode (A): the incident electrons produce characteristic radiation (X)
- ▶ High heat load on the anode: cooling is needed! (W_{in} , W_{out})

Bremsstrahlung

- ▶ An accelerating charged particle produces electromagnetic radiation
- ▶ The total emitted power if the acceleration is parallel to the velocity:

$$P_{a\parallel v} = \frac{q^2 a^2 \gamma^6}{6\pi\epsilon_0 c^3}; \quad \vec{\beta} = \vec{v}/c; \quad \gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

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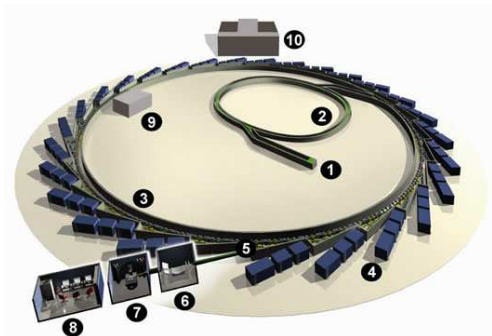
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- ▶ \Rightarrow orbiting charged particle emits electromagnetic radiation
- ▶ **Where do we encounter orbiting charged particles?**

Synchrotron radiation

Electromagnetic radiation detected in the tangential direction of charged particles orbiting on a circular path

1. Electron gun and linear accelerator (linac)
2. Pre-accelerator ring (booster)
3. Storage ring
4. Experiment hall
5. Beamline
6. Optics hutch: mirrors, monochromators etc.
7. Experiment hutch
8. Experiment control room
9. Machine control room
10. Main building



Storage ring

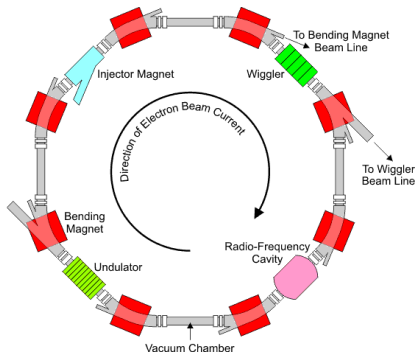
Vacuum chamber: $< 10^{-8}$ mbar

RF cavity: feeding back the emitted energy

Injector magnet: replacement of the absorbed electrons

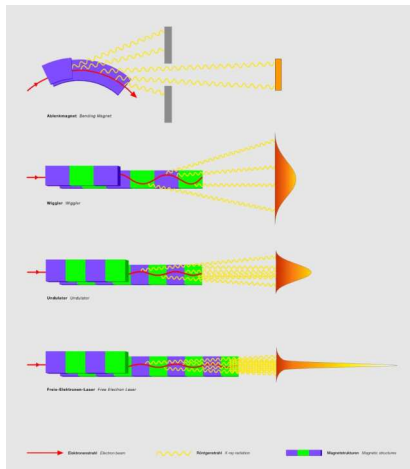
Bending magnets: Circular orbit, producing radiation

Wigglers and undulators: periodic magnets, producing high intensity radiation



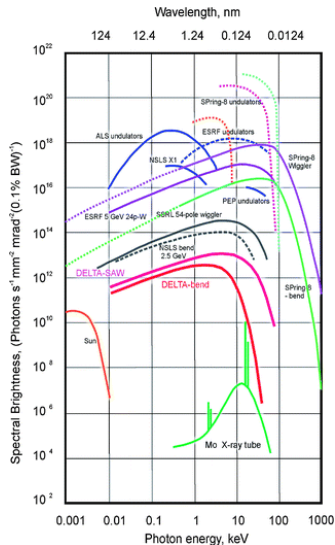
Radiation production in a synchrotron storage ring

- ▶ Charged particles (typically electrons) orbit in bunches: *synchrotrons are pulsed sources*
- ▶ Feeding back lost energy and compacting bunches: RF cavities/resonators
- ▶ Bending magnets: Lorentz-force
- ▶ Wiggler: many bending magnets after each other
- ▶ Undulator: constructive interference of radiation produced in subsequent bends



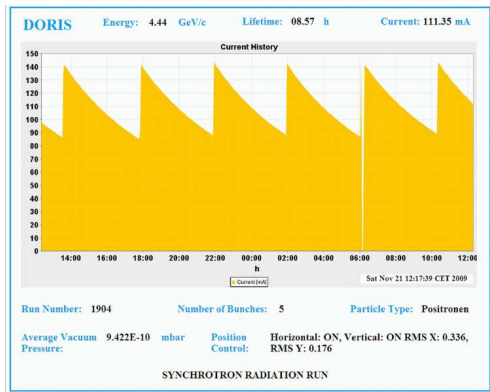
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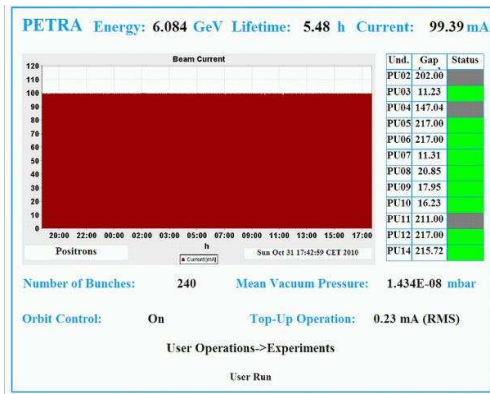
Time structure of synchrotron radiation

- ▶ Intensity is not constant in time
- ▶ Long time scale: replacing the absorbed particles
 - ▶ Occasionally (4-8 hours): “injection”



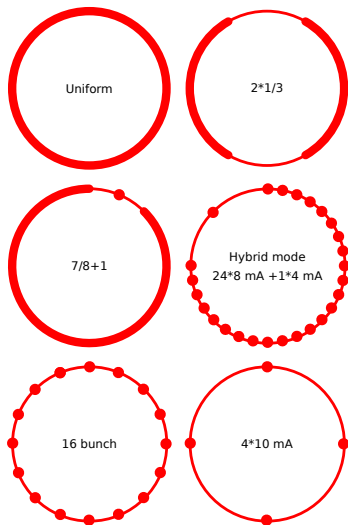
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 - ▶ Continuously: “top-up mode”
- ▶ Short time scale: dispersion of the bunches around the orbit
 - ▶ Time-resolved experiments
 - ▶ Pump-probe techniques



Advantages of synchrotron radiation

High intensity: Short measurement times,
SAXS imaging

Pulsed radiation: time-resolved experiments

Tunable wavelength: ASAXS

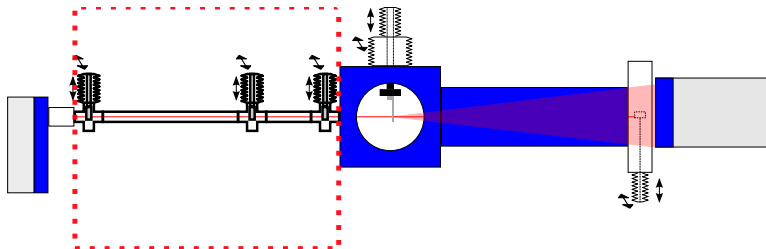
Beamtime proposal system

1. Submit a beamtime proposal: scientific topic, relevance, why do you need a synchrotron. . .
2. Proposal gets refereed
3. Successful proposal: beamtime is scheduled
4. The experiments (1-5 days on-site)
5. Back home, evaluate the data (several GBytes)
6. "da capo al fine"

Advantages of a laboratory SAXS instrument

- ▶ High availability (it is always there)
- ▶ Can be tuned or even rebuilt
- ▶ The same camera, just the source is different
- ▶ Chemistry lab, sample preparation is near
- ▶ Slow measurements, but "infinite" beamtime
- ▶ Preparation for synchrotron measurements
 - ▶ Better beamtime proposal
 - ▶ Preliminary characterization/screening

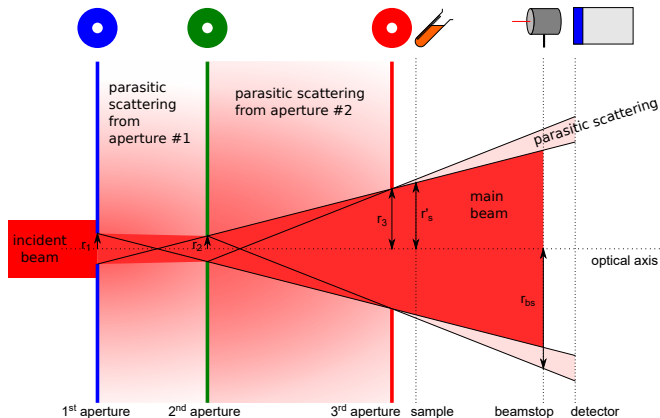
Collimation



Collimation: why do we need that?

- ▶ The scattering cross-section of X-rays is really small
 - ▶ the un-scattered intensity is more than $\times 1000$ as strong!
- ▶ The direct (not scattered) radiation:
 - ▶ may damage the detector
 - ▶ a global read-out detector cannot detect the weaker scattered radiation
- ▶ Differentiation between scattered and non-scattered radiation:
 - ▶ Beam stop before the detector
 - ▶ Parallel beam with a small cross-section
- ▶ Beam shaping:
 - ▶ Optical elements: mirrors, capillaries, X-ray lenses
 - ▶ “Cutting” with slits

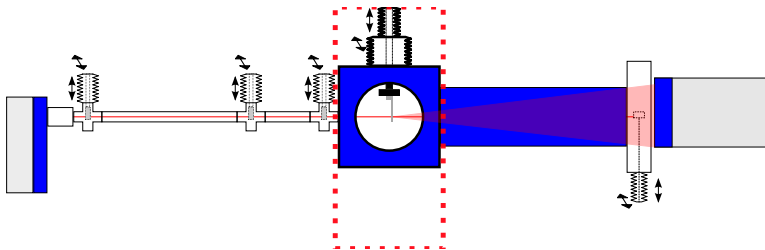
Three aperture collimation scheme



Roles of the apertures

1. Limiting the size of the incoming beam
2. Limiting the divergence
3. Covering the parasitic scattering

Sample environment



Sample environment

Sample environment

- ▶ Air has small-angle scattering
 - ▶ In vacuum
 - ▶ Helium, hydrogen ($\Delta\rho$ small)
 - ▶ Minimizing the in-air beam path
- ▶ *In situ* measurements
 - ▶ Temperature
 - ▶ Shear
 - ▶ Magnetic field
 - ▶ Mixing

Typical sample requirements

Self-carrying solids: homogeneous platelets, cross-section larger than the beam

Liquids: vacuum-safe sample holders (glass/quartz capillaries)
>20 μl

Powders: to be avoided (strong power-law scattering from the surfaces of powder particles)

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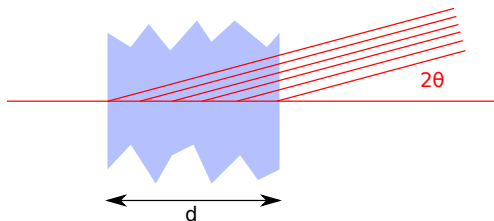
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Ideal sample thickness



- ▶ Scattered and non-scattered rays are partially absorbed by matter
- ▶ Lambert-Beer law: $I(d) = I_0 e^{-\mu d} = I_0 T$
- ▶ Scattered intensity: $I(q, d) \propto I_0 e^{-\mu d} d$
- ▶ Maximizing the scattered intensity: $\frac{\partial I(q, d)}{\partial d} = 0$

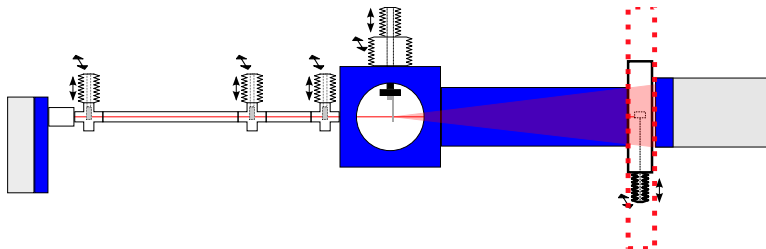
$$\frac{\partial e^{-\mu d} d}{\partial d} = -e^{-\mu d} \mu d + e^{-\mu d} = 0$$

$$1 = \mu d$$

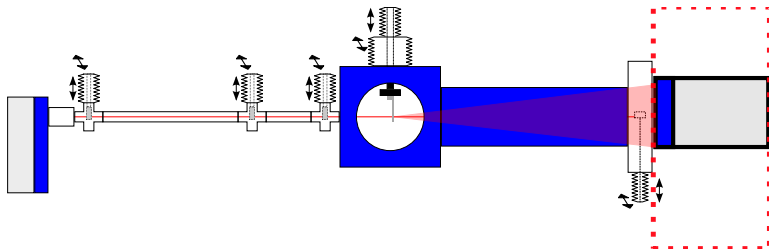
$$d = \boxed{1/\mu}$$

- ▶ Water: $1/\mu \approx 1 \text{ mm}$ with Cu $K\alpha$ radiation (8048 keV, 0.15418 nm)

Beam stop



Detector

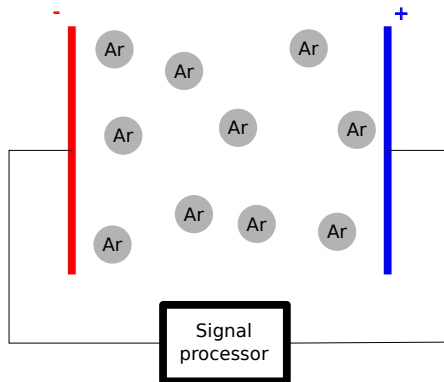


Detector

- ▶ Measuring the angle-dependence of the intensity
- ▶ Energy resolution \leftrightarrow **position resolution**
- ▶ Requirements:
 - ▶ Good position resolution (small pixel size, minimal pixel cross-talk)
 - ▶ Linearity (the detected signal is proportional to the incoming intensity)
 - ▶ High counting speed (frequency)
 - ▶ Low noise
 - ▶ No distortions
 - ▶ Large sensor shape
- ▶ Typical types
 - Gas-filled counters: linearity, low noise, energy selectivity, slow, global readout, large pixels, aging
 - CCD detectors: fast readout, small pixel size, large electronic noise
 - CMOS detectors: fast readout, practically no electronic noise, expensive
 - Image plate: linearity, slow readout, cumbersome handling, aging

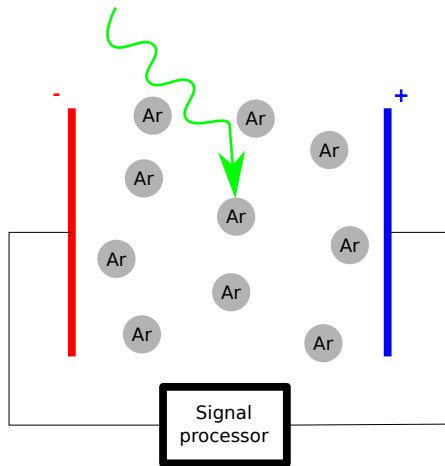
Operation principle of the proportional counter

1. Gas-filled counting chamber



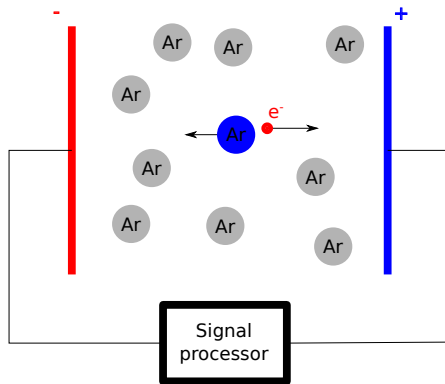
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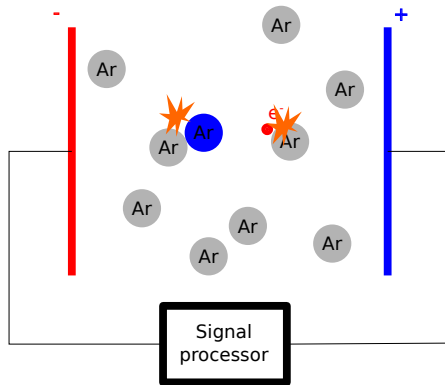
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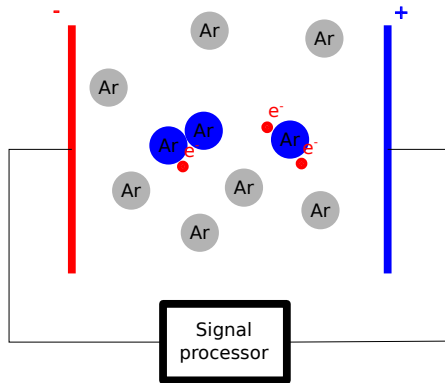
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4. Secondary ionizations



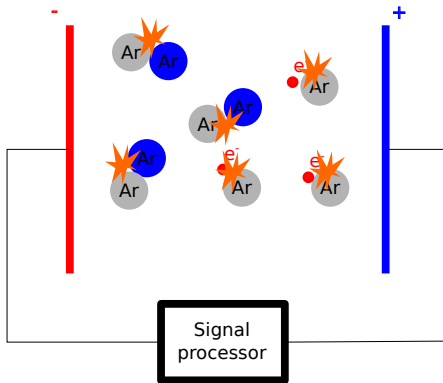
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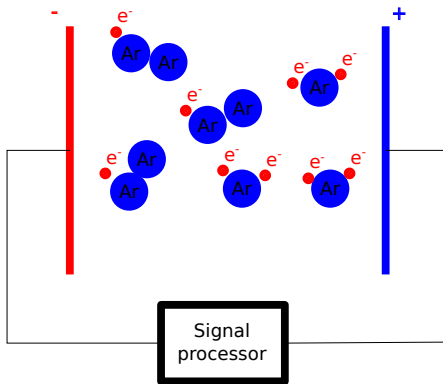
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3. Ions and electrons accelerate towards the electrodes
4. Secondary ionizations
5. Charge multiplication



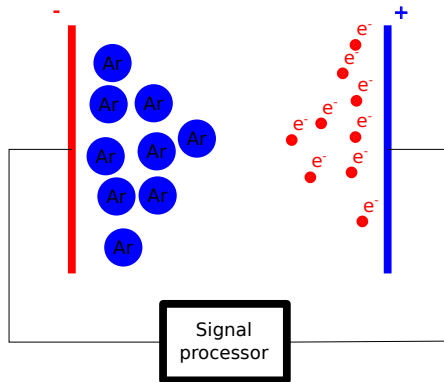
Operation principle of the proportional counter

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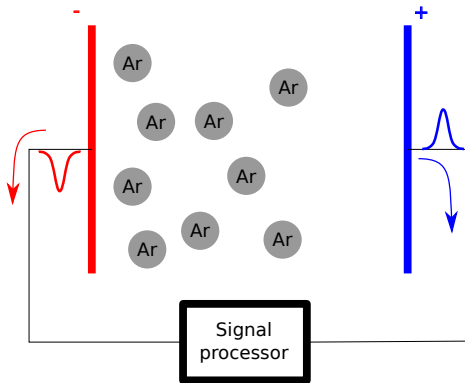
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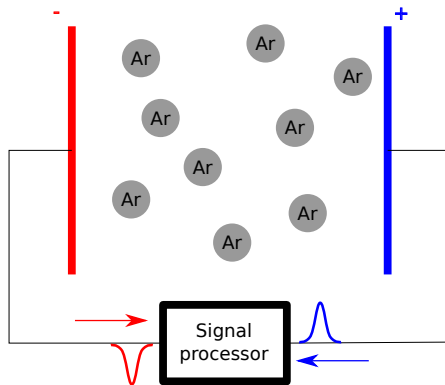
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7. Recombination, pulse signals



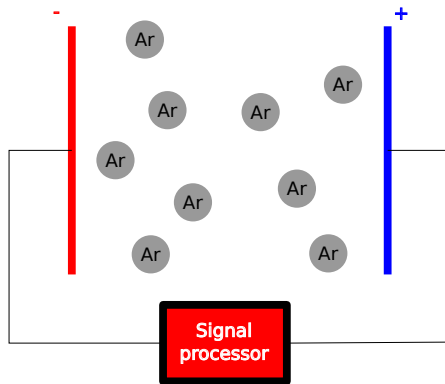
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6. Ion- and electron avalanches hit the electrodes
7. Recombination, pulse signals
8. Integral pulse height $\propto h\nu$
9. Detection of the pulses by the electronics



Outline

Recapitulation

Common SAS camera types

- Characteristic parameters

- Line-focus Kratky camera

- Point focus (pinhole) camera

Main components

- Radiation source

 - X-ray tube

 - Synchrotron

- Collimation

- Sample environment

- Beam stop

- Detector

Two example instruments

- Laboratory SAXS – CREDO

- Synchrotron SAXS – B1 („JUSIFA”)

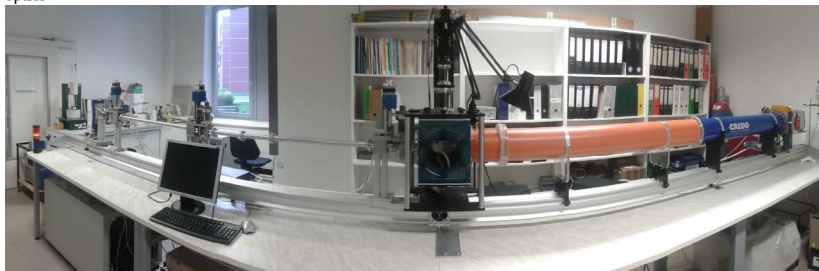
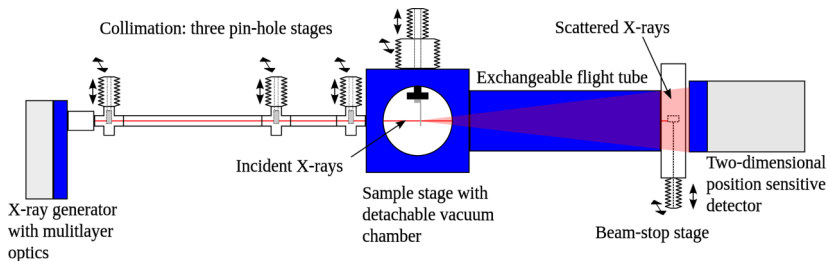
Scheme of an experiment

- Data acquisition

- Corrections and calibrations

Summary

CREDO



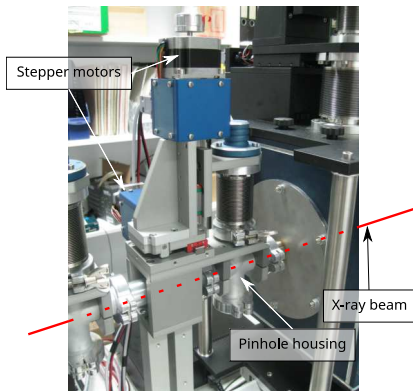
CREDO

- ▶ GeniX^{3D} Cu ULD X-ray generator (30 W, $\lambda = 0.154$ nm, divergence <0.4 mrad HW20%M)



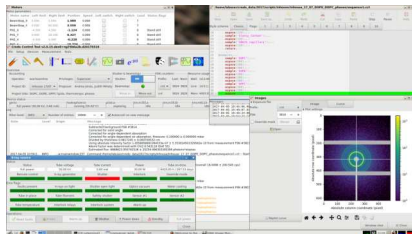
CREDO

- ▶ GeniX^{3D} Cu ULD X-ray generator (30 W, $\lambda = 0.154$ nm, divergence <0.4 mrad HW20%M)
- ▶ Pilatus-300k hybrid pixel CMOS detector (619 \times 478 pixel, 172 μ m, noiseless, independent 20 bit counters for each pixel)
- ▶ 3-pinhole collimation



CREDO

- ▶ GeniX^{3D} Cu ULD X-ray generator (30 W, $\lambda = 0.154$ nm, divergence <0.4 mrad HW20%M)
- ▶ Pilatus-300k hybrid pixel CMOS detector (619 \times 478 pixel, 172 μm , noiseless, independent 20 bit counters for each pixel)
- ▶ 3-pinhole collimation
- ▶ Motorized sample stage, pinholes, beam stop
- ▶ Self-developed, automated data acquisition software
 - ▶ Instrument control
 - ▶ Carrying out the needed corrections and calibrations automatically



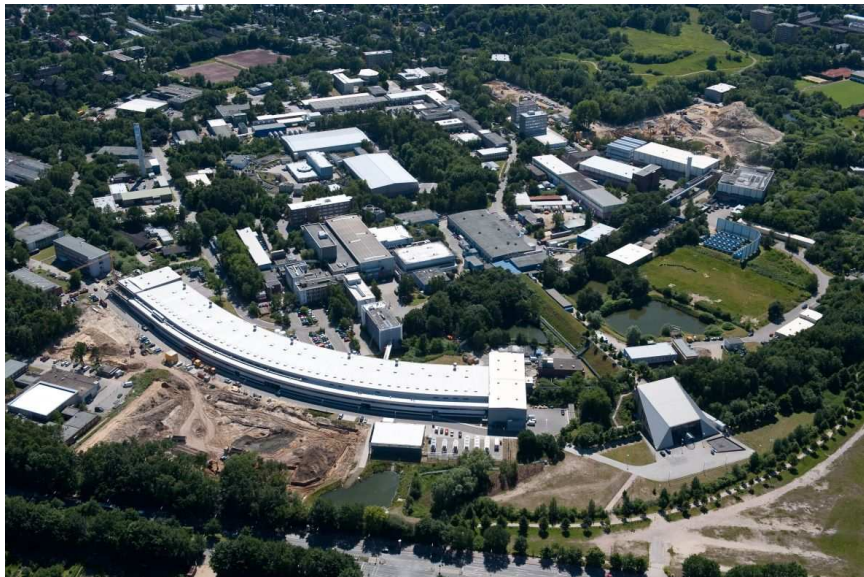
<https://credo.ttk.mta.hu>

B1 („JUSIFA“)

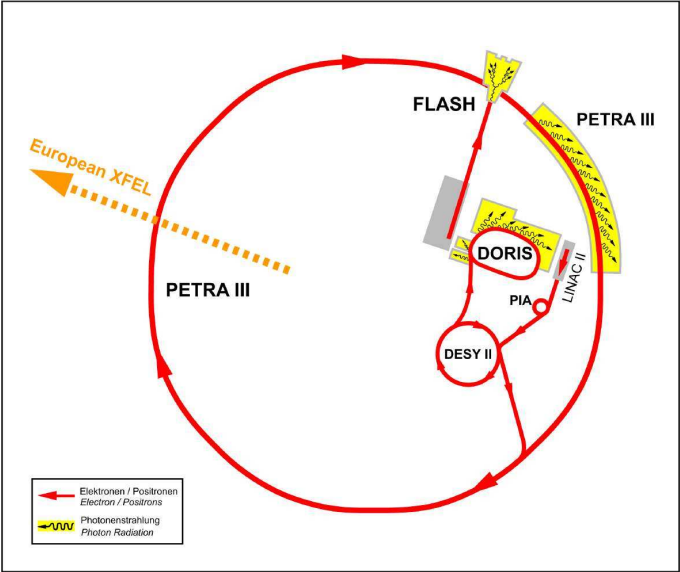


- ▶ Jülich's **U**ser-dedicated **S**cattering **F**acility
- ▶ Deutsches Elektronensynchrotron (DESY), Hamburg
- ▶ DORIS III storage ring
- ▶ dedicated instrument for ASAXS (anomalous SAXS)
- ▶ Gabriel MWPC, Pilatus-300k, Pilatus-1M detectors
- ▶ *1989 - †2012

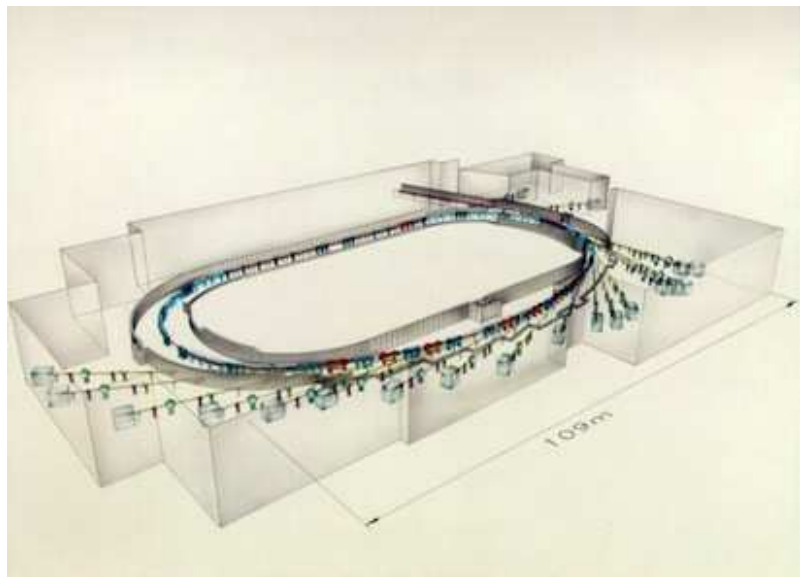
B1 („JUSIFA“)



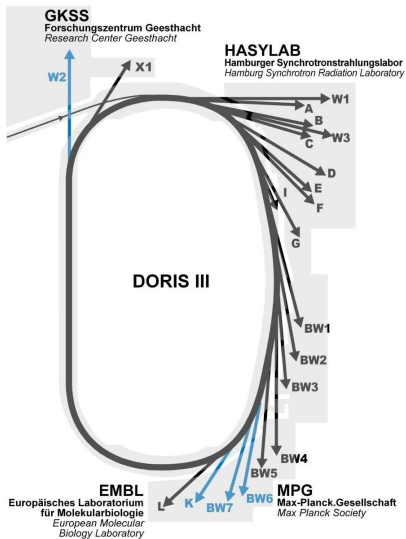
B1 („JUSIFA“)



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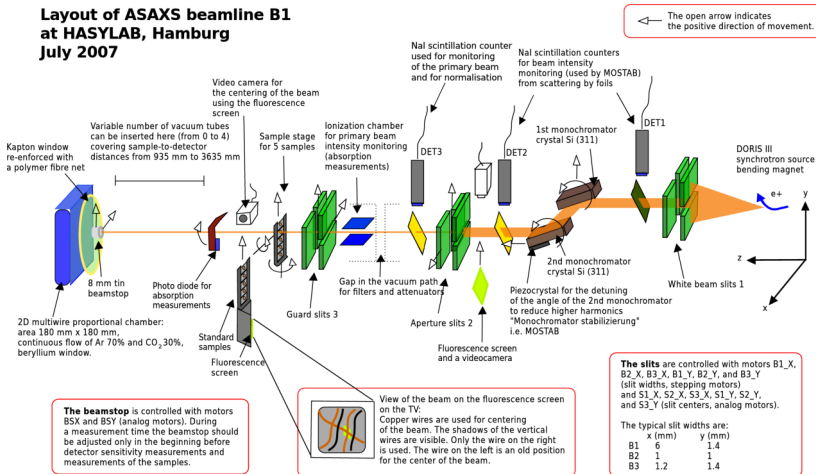


B1 („JUSIFA“)

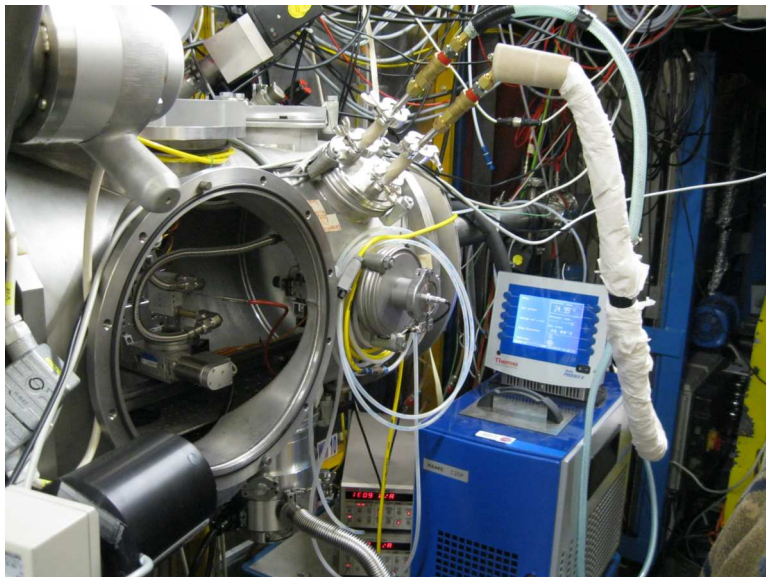


B1 („JUSIFA“)

Layout of ASAXS beamline B1 at HASYLAB, Hamburg July 2007



B1 („JUSIFA“)



B1 („JUSIFA“)



B1 („JUSIFA“)



B1 („JUSIFA“)



B1 („JUSIFA“)



Outline

Recapitulation

Common SAS camera types

- Characteristic parameters

- Line-focus Kratky camera

- Point focus (pinhole) camera

Main components

- Radiation source

 - X-ray tube

 - Synchrotron

- Collimation

- Sample environment

- Beam stop

- Detector

Two example instruments

- Laboratory SAXS – CREDO

- Synchrotron SAXS – B1 („JUSIFA”)

Scheme of an experiment

- Data acquisition

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Summary

Procedure of a “typical” SAXS experiment

1. Turn on the instrument, warm up the X-ray tube (45 minutes)
2. Optimize the geometry (30-45 mins)
 - ▶ Sample-to-detector size, beam stop size \Rightarrow smallest attainable q
 - ▶ Select pinhole sizes and spacings: no parasitic scattering, highest intensity at the sample
3. Sample preparation, capillary filling (1/2-2 hours)
 - ▶ \approx 1 mm borosilicate glass capillaries
 - ▶ Sealing: 2-component epoxy resin / melting
4. Preparation measurements: search for sample motor positions, measure transmissions (30-45 mins)
5. Automatic measurement sequence (several hours / overnight)
 - 5.1 Blank measurements (dark current, empty beam)
 - 5.2 Reference samples (q , $d\sigma/d\Omega$)
 - 5.3 Samples
 - 5.4 Repeat...

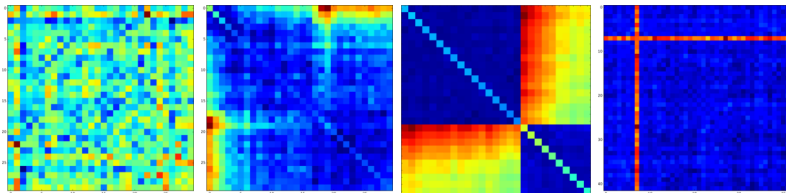
Distribution of the measurement time

It is useful to measure many short exposures instead of one long

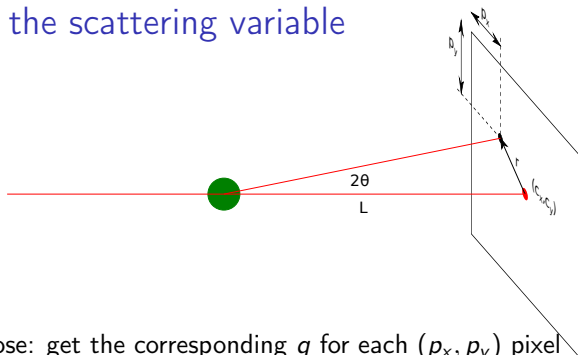
- ▶ Time resolution (TRSAXS)
- ▶ Frequent re-measuring of references
- ▶ Assessment of the stability of the samples and the instrument
- ▶ Excluding affected exposures with statistical tests:
 - ▶ Difference of the j -th and j' -th scattering curve:

$$\Delta_{jj'} = \begin{cases} \sum_k (I_j(q_k) - I_{j'}(q_k))^2 & \text{if } j \neq j' \\ \langle \Delta_{jl} \rangle_{l \neq j} & \text{if } j = j' \end{cases}$$

- ▶ Replacing the diagonal items with row averages: $\Delta_{jj} \rightarrow$ how much does the j -th curve differ from all the others



Calibrating the scattering variable



- ▶ Purpose: get the corresponding q for each (p_x, p_y) pixel
- ▶ If the direct beam would hit the detector at (c_x, c_y) , the pixel size is h and L is the sample-to-detector distance:

$$2\theta = \tan^{-1} \frac{r}{L}; \quad r = h\sqrt{(p_x - c_x)^2 + (p_y - c_y)^2}$$

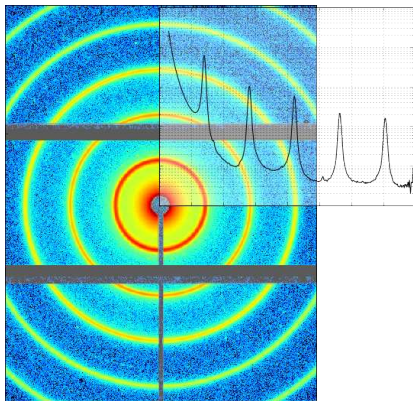
$$q = \frac{4\pi}{\lambda} \sin \left(\frac{1}{2} \tan^{-1} \left(\frac{h\sqrt{(p_x - c_x)^2 + (p_y - c_y)^2}}{L} \right) \right)$$

Calibrating of the scattering variable

- ▶ The sample-to-detector distance is tricky to measure directly
- ▶ Calibration samples: silver-stearate, silver-behenate, SBA15, LaB₆, tripalmitine. . .
 - ▶ high intensity, sharp peaks in the scattering
 - ▶ stable: vs. time and vs. temperature
 - ▶ *peak positions are known*
- ▶ Principle of finding the sample-to-detector distance:
 - ▶ Peak positions are known (q_i)
 - ▶ Measured peak positions in *pixel* units (p_i)
 - ▶ Fitting of the function


$$q = \frac{4\pi}{\lambda} \sin \left(\underbrace{\frac{1}{2} \tan^{-1} (ph/L)}_{2\theta} \right) \rightarrow$$

determine L

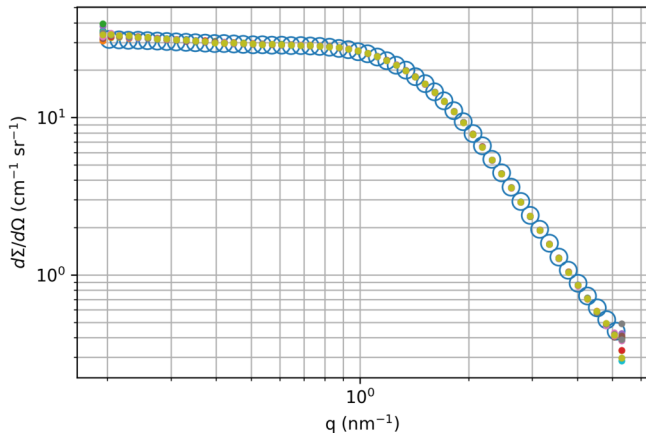


Calibration of the scattering intensity

- ▶ Purpose: scale the count rates to differential scattering cross-section ($\text{cm}^{-1} \text{sr}^{-1}$)
- ▶ Independent from instrumental parameters:
 - ▶ Sample thickness
 - ▶ Beam shape and intensity
 - ▶ Quantum efficiency¹ of the detector
 - ▶ Measurement geometry
- ▶ Many parameters cannot be measured
- ▶ Reference sample:
 - ▶ Strong scattering
 - ▶ “Flat” scattering curve (not sensitive to miscalibrations in q)
 - ▶ Intensity is known in absolute units
 - ▶ Measured with other methods (e.g. glassy carbon, lupolen)
 - ▶ Known from theory (e.g. water, nanoparticle suspension)
- ▶ Measure the reference sample and your samples under the same conditions → the same intensity scaling factor applies

¹The probability of the detection of an incoming photon 

Intensity calibration with glassy carbon



If the curves are appropriately corrected, the scaling factor is the inverse of the beam flux!

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Summary

Summary

- ▶ Types of SAXS instruments
 - ▶ Line focus compact Kratky camera
 - ▶ Pinhole camera
- ▶ Operation principle of the X-ray generator
 - ▶ Characteristic radiation and bremsstrahlung
- ▶ Synchrotrons
 - ▶ Accelerators, storage ring
 - ▶ Insertion devices for beam production
 - ▶ Time structure
- ▶ Main parts of SAXS instruments
 - ▶ Source, detector, sample stage, collimation ...
- ▶ Data collection
 - ▶ corrections, calibrations
 - ▶ data collection strategies (many a little makes a mickle...)

Next lecture: Interpretation of SAXS results with actual examples

Thank you for your attention!

